Problem Set 10

1. What is the output of the following program?

2. Convert problem 1 of Problem Set 7 to the one using functions.

3. Write functions to do the following:

- a. return 1 if number n is prime
- b. return nth fibonacci number
- c. return $n^{th} \mbox{ power of } 2$
- d. return nth prime number
- e. return the sum of all digits of n
- f. return a random number less than n
- 4. Write a function to take two integers n1 and n2 as arguments and:
 - a. return n1 * n2
 - b. return n1ⁿ²
 - c. return 1 if n1 < n2 else 0
 - d. return Ackermann(n1, n2)
 - e. return if n1 and n2 are co-primes

5. Read n rectangle dimensions (length and breadth) from user. A rectangle can fit inside another, if its dimensions are strictly less than the other's. For instance, a rectangle 2x3 can fit into 4x3, as 2<3 and 3<4. Find the largest fitting of rectangles (that is, n1 fits into n2 which fits into n4 which fits into n10, etc.).

6. Solve 8-queens problem. You need to place eight queens in an 8x8 matrix such that no queen attacks any other queen. Two queens attack if they are in the same row or column or diagonal. For instance, one solution is given below. Can you print all solutions?



7. Without using decimal-to-binary conversion, print all binary numbers of lengh 5. Print them with leading zeros first, and later try to remove the leading zeros.

8. Given two sets S1 and S2 of integers, find if S1 is a subset of S2, or S2 is a subset of S1, or they are equal or they are non-comparable.

9. Given a Sudoku problem, solve it. First, in a naive manner, then apply optimizations.

10. For those of you who know the puzzle on grass-goal-tiger with a man wanting to cross a river in a boat with carrying-capacity two, model the puzzle as a programming problem and see if you can generate solutions by executing your C program.