

CS6013 Assignment 1

1. Regular Expressions and DFA

Draw DFAs for the following languages (5 + 5 + 5)

- (a) $L = \{w \in \{a, b, c, d\}^* \mid w \text{ has no repeated letters}\}$
- (b) $L = \{w \in \{1, 2, 3\}^* \mid \text{Number of 2s modulo 2 equal the number of 3s modulo 3}\}$
- (c) $L = \{w \in \{\text{lock}, \text{unlock}, \text{tryLock}\}^* \mid w \text{ denotes a sequence of valid lock operations in Java on a lock}\}$.

Bonus: Write the equivalent REs. (10)

2. CFG

Write the CFG for the following language: (5 + 5 + 5)

- (a) $L = \{w \in \{0, 1\}^* \mid w \text{ contains equal number of 0s and 1s}\}$.
- (b) $L = \{w \in \{0, 1\}^* \mid w \text{ contains unequal number of 0s and 1s}\}$.
- (c) $L = \{w \in \{\text{push}, \text{pop}, \text{top}\}^* \mid w \text{ denotes a sequence of valid stack operations}\}$.

3. Parsing

LL(1) Grammar (30), Parser Implementation (40).

Consider the grammar

```
stmt ... = id(); | stmt stmt | { stmt } | if (id) stmt else stmt
where stmt is the only non-terminal symbol, stmt is the start symbol, and
id ( ) ; { } if else
```

is the list of terminal symbols. The terminal symbol `id` is defined using the regular expression `(letter+)` where `letter` is an ascii character in the interval `a...z`. The grammar generates a subset of the Java statements. Rewrite the grammar into a grammar which is LL(1), and use the rewritten grammar as the basis for implementing a recursive descent parser: write the LL(1) grammar, the FIRST and FOLLOW sets for each nonterminal symbol, and the predictive parsing table, together with an argument that the new grammar is LL(1).